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X-ray Absorption Spectroscopy Studies of a Molecular CO₂-Reduction Catalyst Deposited on Graphitic Carbon Nitride

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Read Online Cite This: J. Phys. Chem. C 2023, 127, 3626-3633 ACCESS III Metrics & More Article Recommendations s Supporting Information 2.8 ABSTRACT: Metal-ligand complexes have been extensively explored as wellient defined molecular catalysts in small molecule activation reactions such as carbon 2.1 Coeffic dioxide (CO_2) reduction. Many hybrid photocatalysts have been prepared by Experiment coupling such complexes with photoactive surfaces for use in solar CO₂ reduction. 1.4 In this work, we employ X-ray absorption near edge structure (XANES) and sor extended X-ray absorption fine structure (EXAFS) spectroscopies, density 0.7

functional theory (DFT) and computational XANES modeling to interrogate the structure of a hybrid photocatalyst consisting of a macrocyclic cobalt complex deposited on graphitic carbon nitride (C_3N_4) . Results show that the cobalt complex binds on C₃N₄ through surface OH or NH₂ groups. By refining the local geometry and binding sites of this well-defined molecular cobalt complex on C_3N_4 ,

Theor ē 0.0 7700 7710 7720 7730 7740 7750 Energy (eV)

we established an important benchmark for modeling a large class of molecular catalysts that can be adapted to in situ/operando studies and further enhanced by applying chemometrics-based approaches and machine learning methods of XANES data analysis.

1. INTRODUCTION

The rising concentration of atmospheric carbon dioxide (CO_2) is thought to be responsible for ocean acidification and other climate changes, such as global warming, sea-level rise, and extreme weather conditions.¹⁻³ The elevated CO₂ level and gradual depletion of fossil fuels have stimulated the development of methods to address the energy crisis and solve environmental problems faced by the whole world.⁴ Solardriven CO₂ reduction is among the most promising approaches to utilize renewable energy to convert CO₂ to valuable chemicals and fuels while mitigating the increasing CO_2 concentration in the atmosphere.^{5–8} Currently known photocatalysts for CO2 reduction include molecular and supramolecular complexes as well as inorganic semiconductors. $^{9-14}$

In recent years, hybrid photocatalysts consisting of welldefined molecular complexes grafted on semiconductor photosensitizers have attracted strong interest for use in solar CO_2 reduction.^{15–21} For example, Kuriki et al.²² fabricated several high-performance hybrid photocatalytic systems with ruthenium complexes on graphitic carbon nitride (C_3N_4) for photocatalytic CO₂ reduction. The ruthenium complexes were derivatized with different functional groups (-H, -COOH, $-PO_3H_{2i}$ and $-CH_2PO_3H_2$) for immobilization on surfaces. However, the explicit binding interactions between the metal complexes and light-absorbing semiconductors were not clearly discussed. In solar fuel research, more catalysts based on earthabundant metals have recently been reported.²³ In particular, there are many studies using cobalt (Co)-based molecular catalysts because of their outstanding performance, low cost, and stability.²⁴⁻²⁸ Reisner and co-workers^{23,29} deposited Co phthalocyanine cyanine on mesoporous carbon nitride with the help of a week $\pi - \pi$ stacking interaction and obtained a turnover number of 90 for CO₂ conversion to CO after 60 h under UV/vis light. In the recent work by Wang and coworkers,³⁰ a Co phthalocyanine complex containing -COOH groups was deposited on C_3N_4 for photocatalytic CO_2 reduction. The -COOH groups enabled high surface coverage of the Co complex and promoted its catalytic property. Robert and co-workers³¹ attached a Co-quaterpyridine molecular complex onto carbon nitride through an amide linkage, which showed a remarkable selectivity (98%) for CO production under visible light.

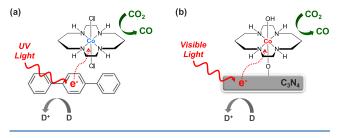
Our recent studies have focused on using $[Co(cyclam)Cl_2]$ -Cl, where cyclam is 1,4,8,11-tetraazacy-clotetradecane, as the molecular catalyst for solar CO₂ reduction. Selective CO₂-to-CO conversion has been achieved using $[Co(cyclam)Cl_2]Cl$ with p-terphenyl as a photosensitizer under UV light irradiation,³² as shown in Scheme 1a. In our previous work,³³⁻³⁶ [Co(cyclam)Cl₂]Cl was deposited on the surfaces of TiO₂ and C₃N₄ for use in photocatalytic CO₂ reduction. In

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Scheme 1. Schematic of CO_2 Reduction on a Macrocyclic Cobalt Catalyst Using (a) *p*-Terphenyl and (b) C_3N_4 as the Photosensitizers. D is an Electron Donor.



this current study, we focus on structural investigation of $[Co(cyclam)Cl_2]Cl$ deposited on C_3N_4 , which is denoted "CoX/C₃N₄" since the axial ligands on the Co center are different from the molecular complex upon surface deposition. As will be discussed, the Cl ligands in $[Co(cyclam)Cl_2]Cl$ could be replaced with -OH groups (Scheme 1b) during the synthesis of CoX/C_3N_4 in the presence of a weak base, triethylamine (TEA).

 C_3N_4 is an interesting material that has been extensively studied in photocatalysis due to its low cost, high thermal and chemical stability, nitrogen-rich structure, and suitable bandgap.^{25,37,38} In photocatalytic CO₂ reduction, triethanolamine (TEOA) is often used as a sacrificial electron donor¹⁰ for C_3N_4 -based materials. Recently, we prepared single atom catalysts by coordinating single Co²⁺ sites on C_3N_4 , in the absence of additional ligands, via a simple microwave method.^{37,39,40} Selective CO₂ reduction under visible-light irradiation was achieved by using such single Co²⁺ sites. However, the single Co²⁺ sites only exist at low cobalt loadings on C_3N_4 ; at high loadings, catalytically inactive CoO_x formed instead of the single Co²⁺ sites. Even at low cobalt loadings, different single Co²⁺ sites might co-exist.⁴⁰

This current study focuses on the structural investigation of CoX/C_3N_4 prepared by depositing $[Co(cyclam)Cl_2]Cl$ on C_3N_4 . Due to the well-defined structure of $[Co(cyclam)Cl_2]Cl$, all the cobalt sites in CoX/C_3N_4 are identical. Furthermore, the use of C_3N_4 as the solid-state photosensitizer enables CO_2 reduction under visible-light irradiation (Scheme 1b).

To obtain atomic-level structural information, we previously employed X-ray absorption spectroscopy (XAS) to characterize transition metal catalysts in both ex-situ and in-situ/ operando studies.^{25,41-45} Specifically, the extended X-ray absorption fine structure (EXAFS) analysis can provide valuable insights into the local geometric structure and coordination environment of the metal sites.46-48 The X-ray absorption near edge structure (XANES) spectra are particularly sensitive to the electronic structure of the metal center and its local environment.⁴⁹⁻⁵² Our recent work³⁶ utilized XANES spectra of CoX/C3N4 to probe possible intermediates during photocatalytic CO₂ reduction. While the chemometrics-based approach for separating between different Co structures coexisting in reaction conditions was successful, the choice of the structural model for using a machine learning - based method of XANES data analysis was guided by human expertise only. To address this and other challenges in studying the catalyst structure and local environment, new data analysis protocols need to be developed.53 In terms of the XANES analysis of atomically dispersed catalysts, one important challenge is the lack of knowledge of multiple possible structures for theoretical XANES modeling. As an important

step towards solving this general speciation problem, in this study, we combine theoretical XANES modeling with density functional theory (DFT) simulations and EXAFS data analysis to further understand the local structure of Co in a well-defined, supported molecular catalyst with demonstrated activity in photocatalytic CO_2 reduction.

2. EXPERIMENTAL

2.1. Materials. Acetonitrile (99.999%) and 1,4,8,11tetraazacyclotetradecane (cyclam, 98%) were obtained from Sigma-Aldrich. Methanol and chloroform (99.8%) were purchased from Pharmco-Aaper. Triethylamine (TEA, \geq 99%) was obtained from Acros. Triethanolamine (TEOA, \geq 99%) and urea (98%) were obtained from Alfa Aesar. All reagents were used without further purification.

2.2. Synthesis of C₃N₄. Graphitic carbon nitride (C_3N_4) was prepared by pyrolysis of urea. In a typical synthesis, 20 g urea was put into a covered crucible and calcined in a muffle furnace at 600 °C for 4 h (ramp rate 5 °C/min). Note: pyrolysis of this urea sample (98% purity) produced a C-doped C_3N_4 sample. The quality of C-doped C_3N_4 may vary due to differences in the composition of commercial urea samples at this purity level. We have reported an improved method to synthesize C-doped C_3N_4 using urea of the highest purity (99.5+%) and dextrose as the source of C dopant.³⁷

2.3. Catalyst Synthesis. The molecular catalyst, [Co-(cyclam)Cl₂]Cl, was synthesized following an established method. To deposit $[Co(cyclam)Cl_2]Cl$ on C_3N_4 , 100 mg C_3N_4 were mixed with a specific amount of $[Co(cyclam)Cl_2]$ Cl in 7.5 mL acetonitrile. Then 65 μ L TEA was added to the mixture, which was subsequently stirred for 2 h. The mixture in a capped reaction vessel was placed in a CEM Discover single-mode microwave reactor and was heated to 80 °C for 120 min. After the microwave reaction, the resulting precipitate was recovered by centrifugation and washed twice with chloroform, methanol, and acetonitrile, respectively. After drying at room temperature, a photocatalyst, denoted "CoX/C₃N₄", was obtained.

2.4. Materials Characterization. Elemental analysis was conducted by acid digestion, followed by quantification using a Varian Vista AX induced coupled plasma atomic emission spectrometer (ICP-AES). X-ray diffraction (XRD) patterns of powder samples were collected on a Rigaku X.D.S. 2000 diffractometer using nickel-filtered Cu K α radiation ($\lambda = 1.5418$ Å). Scanning electron microscopy (SEM) images were collected on an Amray 3300FE field emission SEM with P.G.T. Imix-PC microanalysis system. Ultraviolet-visible (UV–Vis) spectra were obtained on a Cary 50 Bio spectrophotometer. A Barrelino diffuse reflectance probe was used to collect UV–Vis spectra of powder samples using BaSO₄ as a standard. Fourier transform infrared (FTIR) spectra were collected on a Thermo Nicolet iS10 FTIR spectrometer.

2.5. Photocatalytic Testing. In photocatalytic CO₂ reduction, a specific amount (1.0 mg) of catalyst was dispersed in a 4.0 mL acetonitrile solution containing TEOA (acetonitrile: TEOA = 4:1 v/v) in a quartz test tube (Scheme S1). In the testing using a physical mixture of $[Co(cyclam)Cl_2]$ Cl and C_3N_4 , the reaction solution contained 13 μ L methanol for dissolving $[Co(cyclam)Cl_2]$ Cl. Prior to photocatalytic testing, the reaction solution was bubbled with CO₂ (99.999%, Airgas) in the dark for 20 min. The reaction solution was then irradiated with a halogen lamp equipped with a water filter. Light intensity on the reaction solution was

fixed at 200 mW/cm². The head space above the reaction solution was sampled with a gas-tight syringe at different time intervals for product analysis using an Agilent 7820 GC equipped with a thermal conductivity detector. detector and a 60/80 Carboxen-1000 packed column (Supelco).

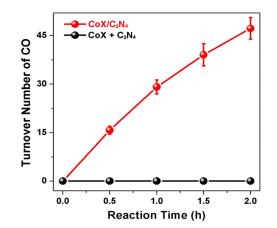
2.6. X-ray Absorption Spectroscopy. X-ray absorption spectra at Co K-edge were taken at the beamline 7-BM (QAS) of NSLS-II at Brookhaven National Laboratory. An Si (111) double crystal monochromator was used. CoX/C_3N_4 was measured in fluorescence mode. The raw XAFS spectra were analyzed utilizing the Athena and Artemis interfaces of the Demeter software package.⁵⁴ Theoretical XANES spectra were calculated using FEFF code (version 9.6.4).⁵⁵ The input parameters are provided in the SI.

2.7. Computational Modeling. The Vienna Ab initio Simulation Package^{56–59} (VASP) version 5.4.1 was used for all Density Functional Theory (DFT) calculations. The electronion interactions were described by the Perdew–Burke–Ernerhof⁶⁰ (PBE) exchange-correlation function with the projected augmented-wave method^{61,62} (PAW). The DFT-D3 method⁶³ with Becke–Jonson damping⁶⁴ was used to consider the van der Waals interactions. The cut-off energy of the plane wave basis was chosen to be 700 eV. The energy convergence criterion was set to be 10^{-6} eV per unit cell. The Gaussian smearing with $\sigma = 0.1$ eV was used for all calculations and the maximum optimization step-size was at 0.4 Bohr. A 1 \times 1 \times 1 Monkhorst–Pack type k-point grid⁶⁵ was used to sample the Brillouin zone during the geometry optimization.

3. RESULTS AND DISCUSSION

The hybrid photocatalyst in this study, CoX/C_3N_4 , was prepared following a microwave method as described in the experimental section. A weak base, TEA, was used to facilitate the binding of $[Co(cyclam)Cl_2]Cl$ on C_3N_4 (Figure S1 in the Supplementary Information). A negligible amount of [Co- $(cyclam)Cl_2]Cl$ was deposited on C_3N_4 in the absence of TEA. In this present study, we focus on a CoX/C_3N_4 sample with a loading of 0.018 µmol cobalt per 1 mg C_3N_4 . At this level of cobalt loadings, the presence of $[Co(cyclam)Cl_2]Cl$ on C_3N_4 was not seen using X-ray powder diffraction (Figure S2), UV– Vis (Figure S3), infrared spectroscopy (Figure S4), or microscopy (Figure S5). Instead, XAS appeared to be a highly sensitive technique to confirm the presence of cobalt in CoX/ C_3N_4 , as will be discussed later.

The synthesized CoX/C₃N₄ was evaluated in photocatalytic CO₂ reduction using TEOA as a sacrificial electron donor. A halogen lamp was used as the light source to provide photons with wavelengths in the range of 350-800 nm (Figure S6). Under the experimental conditions employed in this study, CO and H₂ were detected by gas chromatography as the major products. Turnover numbers (TONs) were calculated by taking the ratio between the amounts of products and the amount of Co present in the reaction suspension. After photocatalysis for 2 h, TONs of 47 and 17 were obtained for CO and H₂, respectively, representing a selectivity of 74% towards CO production. A TON of more than 160 for CO production was obtained after photocatalysis for an extended period using CoX/C_3N_4 under visible-light irradiation ($\lambda >$ 420 nm, Figure S7). Furthermore, the synthesized CoX/C_3N_4 demonstrated reasonable recyclability in photocatalysis (Figure S8). Under the same conditions, no CO was produced using a physical mixture of $[Co(cyclam)Cl_2]Cl$ and C_3N_4 (Figure 1) or using bare C₃N₄.



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Figure 1. CO production in photocatalytic CO₂ reduction using 1.0 mg CoX/C₃N₄ (red), prepared by the microwave method, and the simple mixture of 1 mg C₃N₄ and [Co(cyclam)Cl₂]Cl (black). In both tests, the amount of [Co(cyclam)Cl₂]Cl was 0.018 μ mol.

The results shown in Figure 1 clearly indicate the key role of attaching $[Co(cyclam)Cl_2]Cl$ on C_3N_4 in enabling photocatalysis using CoX/C_3N_4 . In order to obtain detailed structural information on such surface attachment, CoX/C_3N_4 in the powder form was investigated using XANES and EXAFS. Figure 2 shows the Co K-edge XANES spectrum of

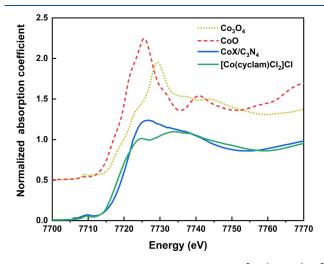


Figure 2. Normalized Co K-edge XANES spectra of $[Co(cyclam)Cl_2]$ Cl (green), CoX/C_3N_4 (blue), and two Co oxide samples as references.

 CoX/C_3N_4 , which has different features from that of $[Co(cyclam)Cl_2]Cl$. Such differences suggest that the coordination environment of cobalt significantly changed upon depositing $[Co(cyclam)Cl_2]Cl$ on C_3N_4 . Based on prior studies,^{33–36} we hypothesize that the two axial Cl ligands of $[Co(cyclam)Cl_2]Cl$ were replaced with one OH group and one surface -O- or -NH- group upon deposition on C_3N_4 through the microwave synthesis in the presence of TEA. In the following context, we combine theoretical XANES modeling with DFT simulations and EXAFS data analysis to test our hypothesis.

In the proposed structure of CoX/C_3N_4 , the "CoX" unit differs from $[Co(cyclam)Cl_2]Cl$ in that it contains a hydroxyl group instead of the Cl ligand. In addition, the CoX/C_3N_4 complex poses a strong challenge to the task of XANES

modeling because of the lack of knowledge about specific binding sites and local geometry. DFT simulations were performed to obtain possible structures of CoX anchored on C_3N_4 , which is known to contain surface NH₂ and OH groups. Other surface functional groups on C_3N_4 , such as secondary amine groups, were also considered as potential binding sites in our DFT simulations but attempts to obtain stable structures on such sites failed. Therefore, the anchoring of CoX to C_3N_4 through either a surface -NH- or -O- group represents the most probable modes, and their optimized structures are shown in Figures 3 and 4, respectively. The

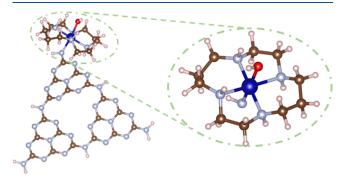


Figure 3. DFT optimized structure of CoX attached to C_3N_4 through a nitrogen atom. Color scheme: Co (blue), N (silver), C (brown), O (red), and H (pink).

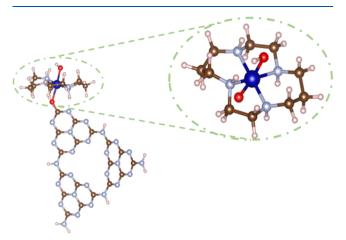


Figure 4. DFT optimized structure of CoX attached to C_3N_4 through an oxygen atom. Color scheme: Co (blue), N (silver), C (brown), O (red), and H (pink).

optimized structures shown in Figures 3 and 4 have similar energies and distances between the Co center of CoX and C_3N_4 . In particular, the Co–N (N on C_3N_4) bond length in the structure shown in Figure 3 is predicted to be 1.96 Å, while the Co–O (O on C_3N_4) bond length in the structure shown in Figure 4 is calculated to be 2.00 Å.

After obtaining the DFT-optimized structural coordinates (see the output files in the VASP format in the Supplementary Information), we used them as a basis for theoretical XANES modeling. In such theoretical studies, the experimental XANES spectrum of $[Co(cyclam)Cl_2]Cl$ was chosen as a standard to optimize the FEFF parameters for simulating the spectra of CoX on C_3N_4 . Both the experimental and theoretical XANES spectra of $[Co(cyclam)Cl_2]Cl$ are shown in Figure 5. As can be seen from Figure 5, the theoretical spectrum of $[Co(cyclam)Cl_2]Cl$

Cl₂]Cl contains all four key features (A, B, C, and D) of the experimental spectrum.

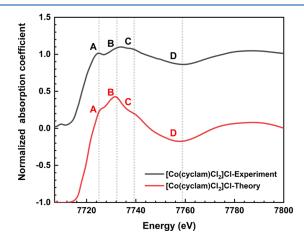


Figure 5. Experimental and simulated XANES spectra of Co atoms in $[Co(cyclam)Cl_2]Cl$.

Theoretical XANES spectra of the DFT – optimized structures shown in Figures 3 and 4 were then calculated and the results are shown in Figure 6. A strong difference

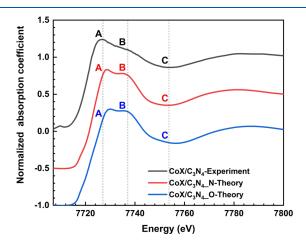


Figure 6. Experimental XANES spectrum of CoX/C_3N_4 (top), and simulated XANES spectra of CoX using DFT optimized structures shown in Figure 3 (middle) and Figure 4 (bottom).

between the experimental data for $[Co(cyclam)Cl_2]Cl$ and CoX/C_3N_4 (Figure 2) is captured by the difference between their corresponding theoretical spectra (Figures 5 and 6). As can be seen from Figure 6, both simulated XANES spectra are in good qualitative agreement with the experimental XANES spectrum of CoX/C_3N_4 . However, it remains unclear whether CoX is attached to C_3N_4 through a nitrogen or oxygen atom, based on the results shown in Figure 6.

We further analyzed EXAFS spectra to gain quantitative information on the structure of CoX/C_3N_4 and correlate with the predictions by DFT-XANES analyses. Figure 7 shows the Co K-edge EXAFS spectra of $[Co(cyclam)Cl_2]Cl$ and CoX/C_3N_4 in *r*-space. Both spectra display characteristics associated with single cobalt sites, compared with those of cobalt oxides. In the spectrum of $[Co(cyclam)Cl_2]Cl$, the first peak is seen at ca. 1.55 Å (uncorrected for the photoelectron phase shift). In contrast, the first peak is around 1.35 Å in the spectrum of CoX/C_3N_4 . This shift upon surface deposition can be

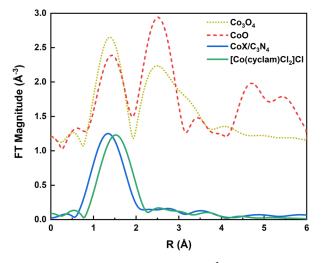


Figure 7. Fourier transform magnitudes of k^2 -weighted Co K-edge EXAFS spectra of $[Co(cyclam)Cl_2]Cl$ (green), CoX/C_3N_4 (blue), and two Co oxides. The k-range from 2 to 7 Å⁻¹ and k^2 weighting were used in the Fourier transform.

explained by our proposed structures shown in Figures 3 and 4. Specifically, the peak in the spectrum of CoX/C_3N_4 corresponds to Co–N (bond length ~ 1.98 Å) and Co–O (bond length ~ 1.92 Å) contributions from the first shell.⁶⁶ The peak in the spectrum of $[Co(cyclam)Cl_2]Cl$ between 1 and 2 Å (uncorrected for the photoelectron phase shift) is contributed by the Co–Cl (bond length ~ 2.25 Å) and Co–N (bond length ~ 1.98 Å) pairs.

Therefore, the difference in the spectra of $[Co(cyclam)Cl_2]$ Cl and CoX/C_3N_4 shown in Figure 7 originated from the replacement of Cl ligands with N/O-containing ligands upon depositing $[Co(cyclam)Cl_2]Cl$ on C_3N_4 .

The EXAFS spectra were analyzed by conventional Levenberg-Marquardt nonlinear least squares method, in which FEFF6 theory was fit to the experimental data while varying adjustable parameters, such as coordination numbers, bond lengths and their variances. The Co foil measured at the same beamline was first analyzed to obtain the passive electron reduction factor S_0^2 (0.61), which is used to fitting the spectra of all samples. Table 1 summarizes fitting parameters obtained for the EXAFS analysis of $[Co(cyclam)Cl_2]Cl$ and CoX/C_3N_4 (Figure 8). For [Co(cyclam)Cl₂]Cl, the Co-Cl and Co-N scattering paths were chosen to fit the first peak. The resulting coordination numbers corresponding to Co-N and Co-Cl bonds are 3.5 ± 1.2 and 2.0 ± 1.2 , respectively. The Co-N and Co–Cl bond lengths were obtained to be 1.94 ± 0.04 Å and 2.25 \pm 0.04 Å, respectively, in excellent agreement with previously published results for a similar macrocyclic cobalt compound.⁶⁷ The Co-O scattering path was chosen to fit the first peak of CoX/C3N4 for the quantitative EXAFS data analysis. The coordination number of Co-O nearest neighbors was found to be 6.3 ± 1.4 .

In this study, results from theoretical XANES modeling and EXAFS data analysis strongly support the DFT optimized structures (Figures 3 and 4). Therefore, Co binding to C_3N_4 via surface N/O atoms represents a plausible model describing the anchoring of CoX on C_3N_4 , even though our results were not able to distinguish between contributions from N and O atoms. As mentioned earlier, attaching CoX to the light-absorbing C_3N_4 is critical to the CO₂-reduction activity demonstrated by CoX/C₃N₄ (Figure 1).

It is worth noting that CoX/C_3N_4 likely underwent some structural changes under the photocatalytic conditions employed in this study, despite its demonstrated recyclability (Figure S8). Figures S9 and S10 show the XAS spectra of CoX/C_3N_4 before and after photocatalysis. Some minor differences are seen in the comparison between the spectra. While it is difficult to say what exactly happened to CoX upon photocatalysis, it is clear that there is no evidence of Co reducing (Figure S9) or aggregation (Figure S10). Our future work includes detailed mechanistic studies of light-induced electron transfer and photostability of CoX/C_3N_4 using timeresolved techniques, as well as coupling other Co-based molecular catalysts⁶⁸ with C_3N_4 for photocatalysis.

4. CONCLUSIONS

In summary, we have synthesized a hybrid photocatalyst by depositing a macrocyclic cobalt complex on light-absorbing C_3N_4 . We combined theoretical XANES modeling with DFT simulations and EXAFS data analysis to probe the structure of the hybrid photocatalyst. Our results indicate that surface attachment of the cobalt complex likely occurs by replacing two axial Cl ligands with one OH group and one surface NH or O group during the synthesis in the presence of a weak base. Our study provides molecular level insights into the structures of this type of hybrid photocatalyst consisting of metal–ligand complexes on heterogeneous surfaces.

One key result of our work is a new XANES data analysis protocol that relies on the application of DFT for selecting candidate structures for Co K-edge XANES modeling for the hybrid photocatalyst bound to the support. The lack of knowledge of the geometry of the catalyst-support sites hampers such studies in which atomically dispersed catalysts of size-selective clusters are analyzed by "inverting" their XANES spectra. This method opens a new opportunity for structural analysis of such photocatalysts using a machine learning approach.^{69,70} Namely, multiple spectra calculated theoretically may be used for training a neural network classifier, similar to an analogous approach developed recently for predicting new topological insulators.⁷¹ Such a classifier will be used for interpreting the spectra of different hybrid photocatalysts in terms of different classes of local structure and local geometry of the support, for subsequent structural refinement. In comparison, current efforts are mostly limited to chemometrics-based approaches and require a large number of experimental spectra for such a classification.^{36,7}

Table 1. Fitting Parameters for $[Co(Cyclam)Cl_2]Cl$ and CoX/C_3N_4 : The Neighboring Pairs, their Coordination Numbers, Distances and Mean Square Relative Displacements, and the Correction to the Photoelectron Energy Origin

samples	paths	coordination number	<i>R</i> (Å)	σ^2 (Å ²)	ΔE (eV)
[Co(cyclam)Cl ₂]Cl	Co-N	3.5 ± 1.2	1.94 ± 0.04	0.000 ± 0.007	1 ± 4
	Co-Cl	2.0 ± 1.2	2.25 ± 0.04	0.000 ± 0.007	1 ± 4
CoX/C_3N_4	Co-O	6.3 ± 1.4	1.91 ± 0.02	0.009 ± 0.005	1 ± 4

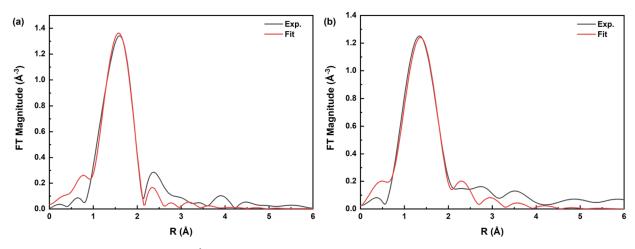


Figure 8. Fourier transform magnitudes of k^2 -weighted Co K-edge EXAFS spectra of (a) $[Co(cyclam)Cl_2]Cl$ and (b) CoX/C_3N_4 and their theoretical fits. The *k*-range is from 2 to 7 Å⁻¹. The *r*-ranges used for fitting the data for $[Co(cyclam)Cl_2]Cl$ and CoX/C_3N_4 were 1.1–2.8 Å and 1.1–2.6 Å, respectively.

ASSOCIATED CONTENT

Supporting Information

The Supporting Information is available free of charge at https://pubs.acs.org/doi/10.1021/acs.jpcc.2c08587.

Supplementary figures of additional characterization data, DFT-optimized structural coordinates, and input parameters for XANES simulation (PDF).

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Notes

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