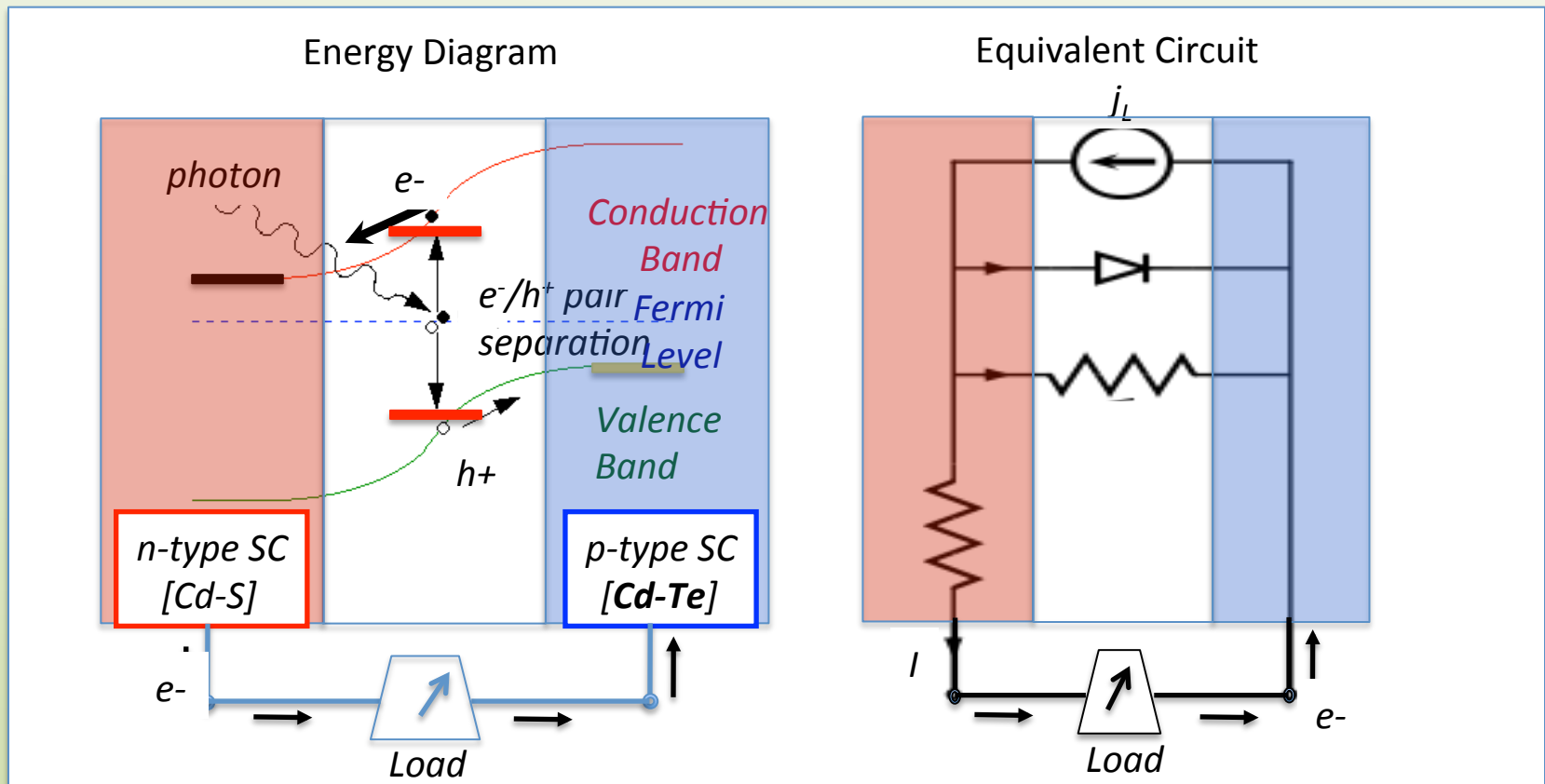


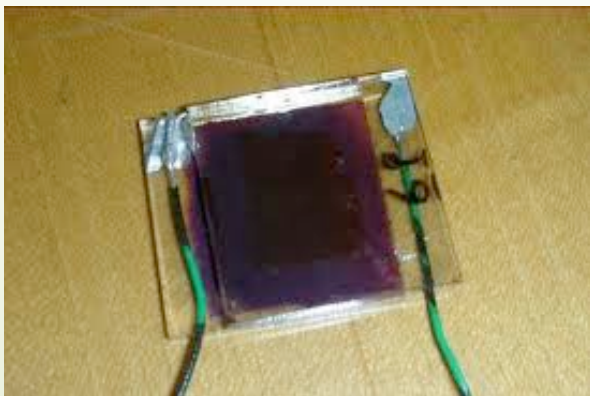
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Modeling Photovoltaic Solar Cells Traditional Photovoltaic Solar Cells

First and Second Generation: p-n junctions



[The Power of the Sun](#): Walter Kohn's Description of Photovoltaic Solar Cells



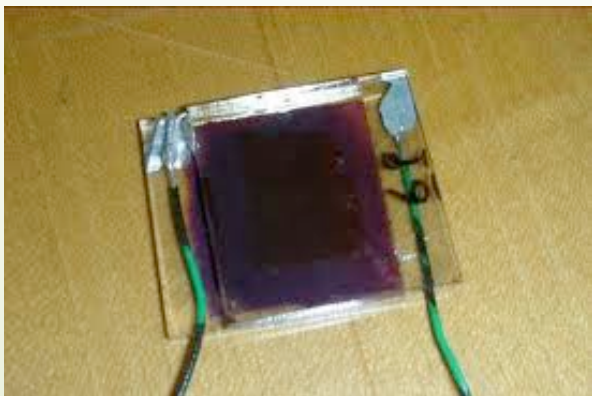
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Section II

Prof. Victor S. Batista

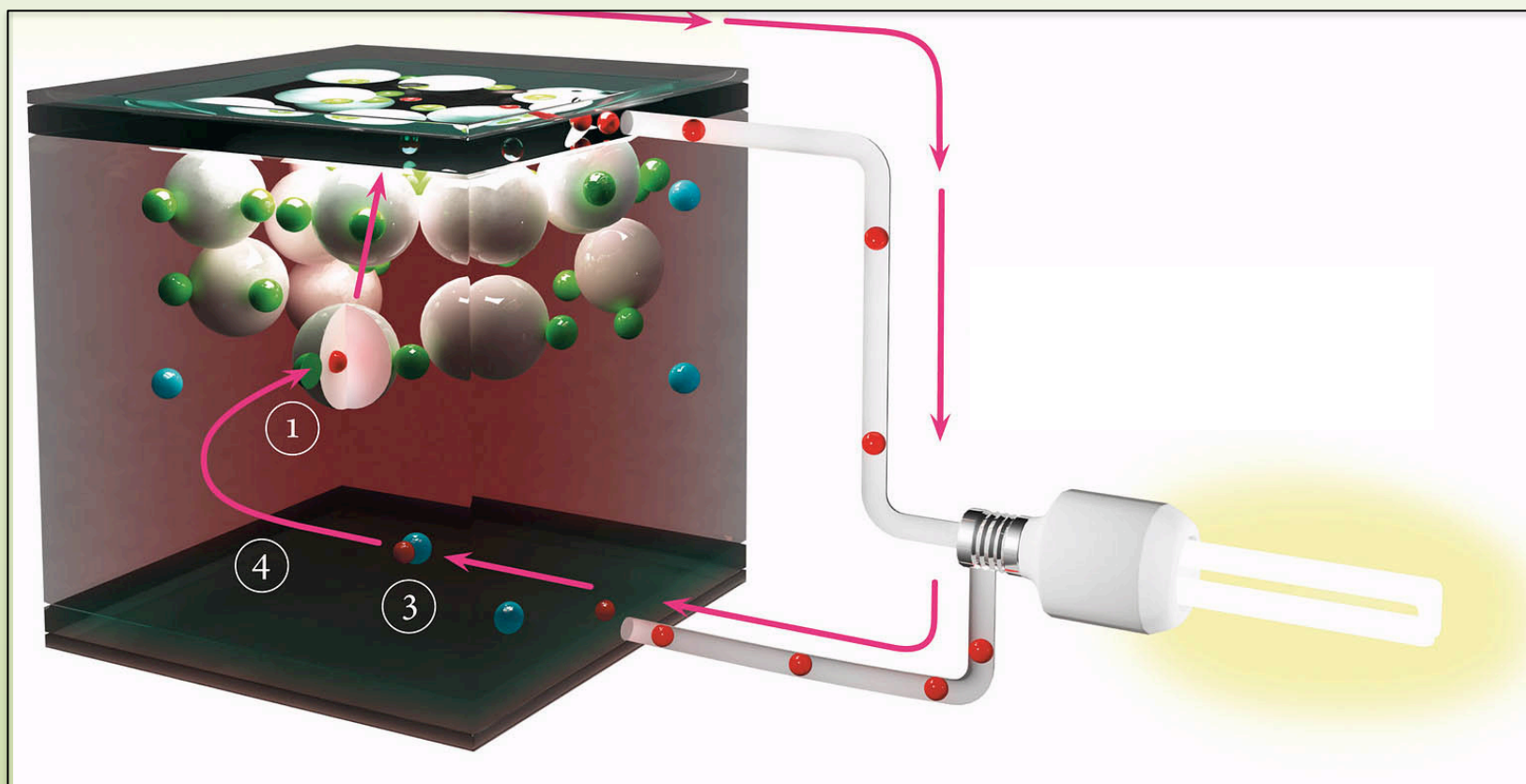
Computational Modeling and Physical Principles

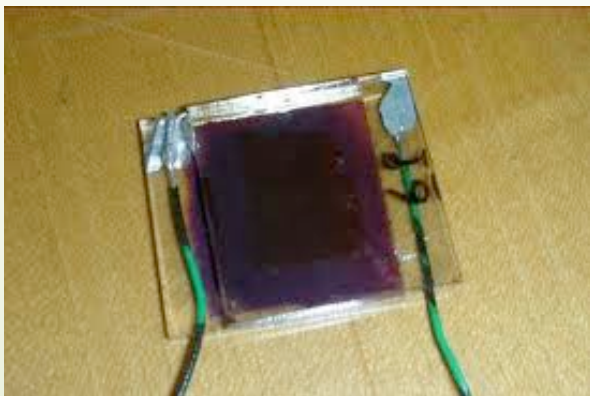
- Computational design and characterization
- Solar cells for electricity
- Photocatalysis, biomimetic water oxidation
- Hydrogen economy



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[Dye-Sensitized Solar Cells](#)
[Third Generation Photovoltaic Solar Cells](#)

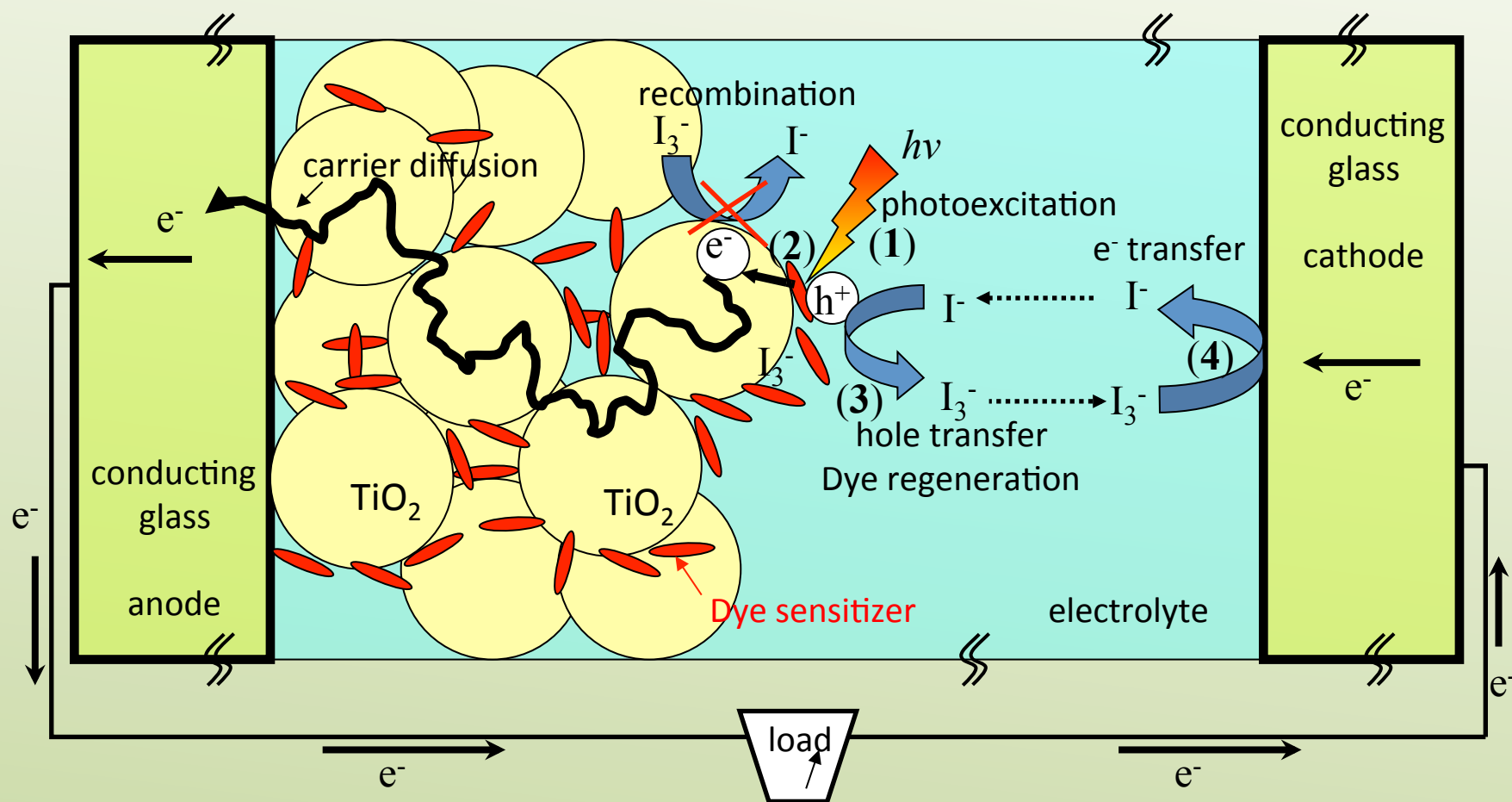


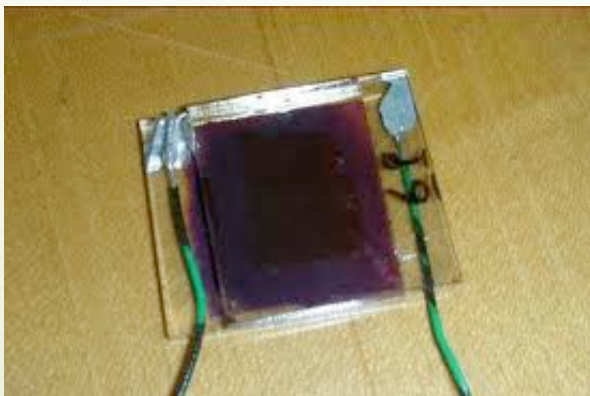


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Modeling Dye-Sensitized Solar Cells

Photoconversion in 4 steps: (1)-(4)

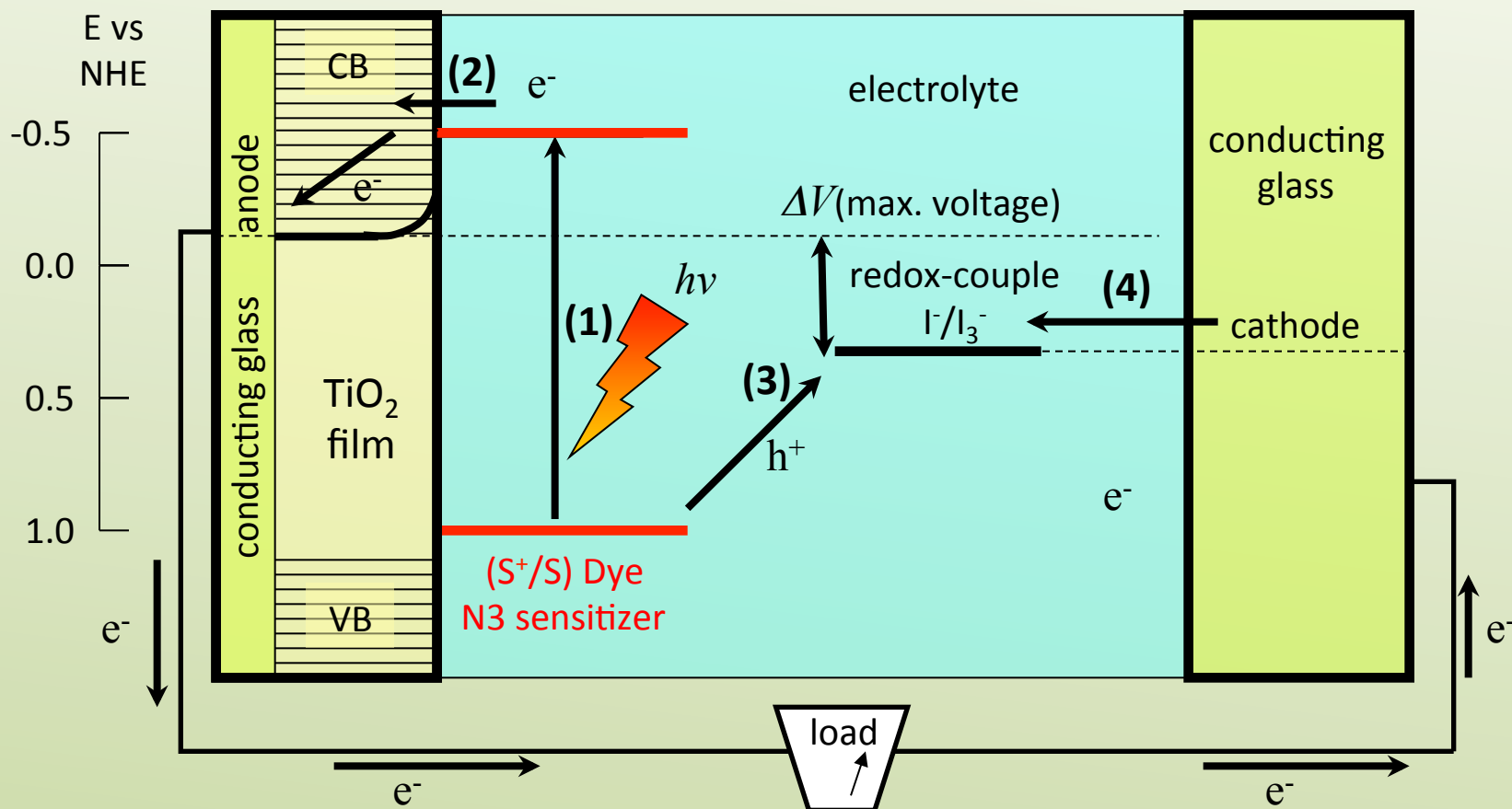


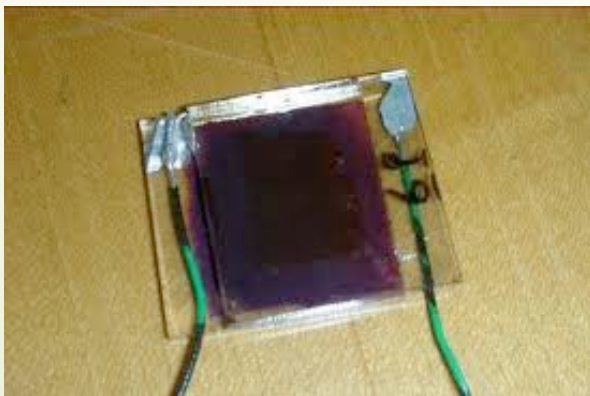


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Modeling Dye-Sensitized Solar Cells

Photoconversion: Energy Diagram

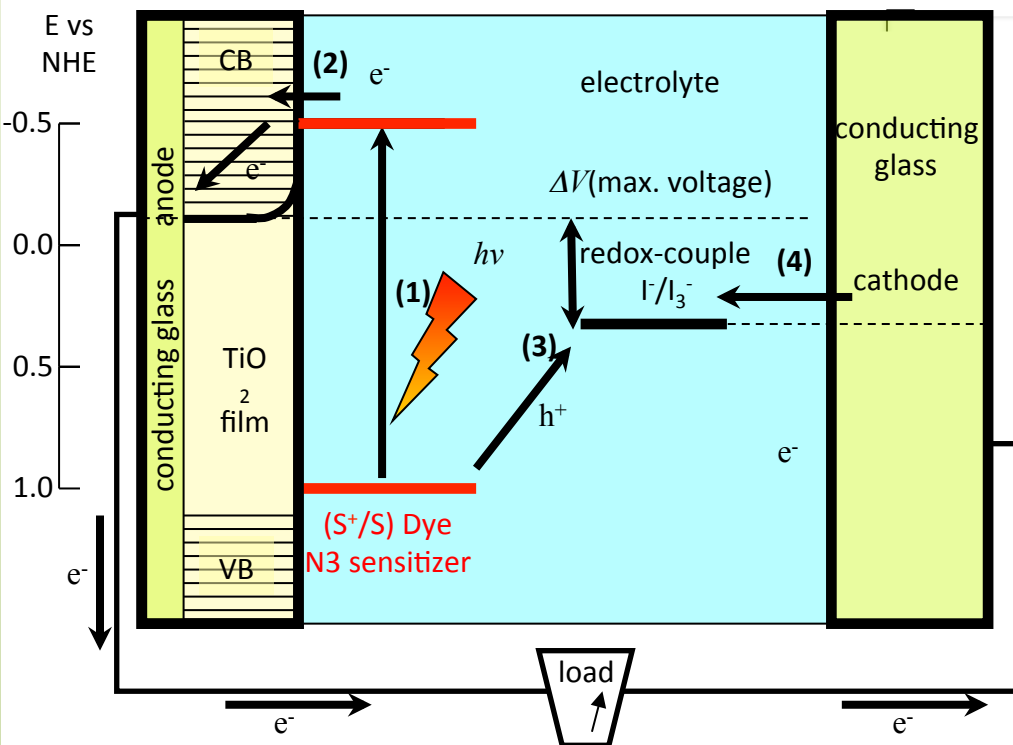




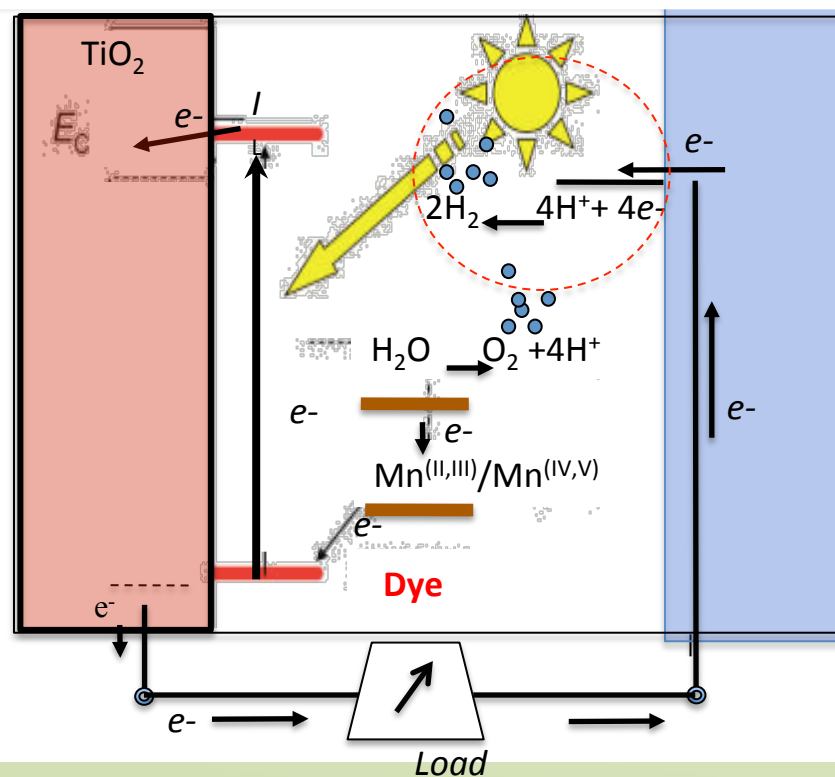
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Modeling Dye-Sensitized Solar Cells
Photoconversion into Chemical Bonds: Fuel

Solar-to-Electricity Conversion

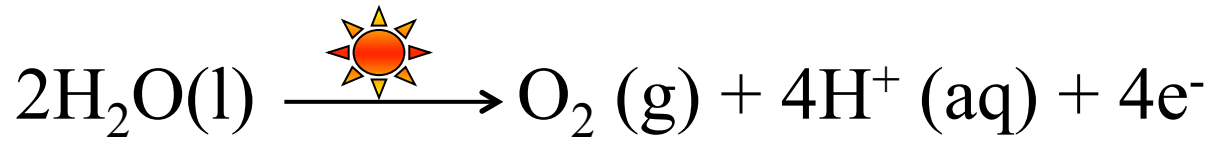


Solar-to-Fuel (H₂) Conversion

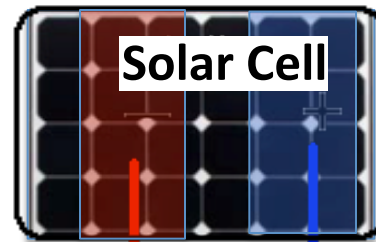
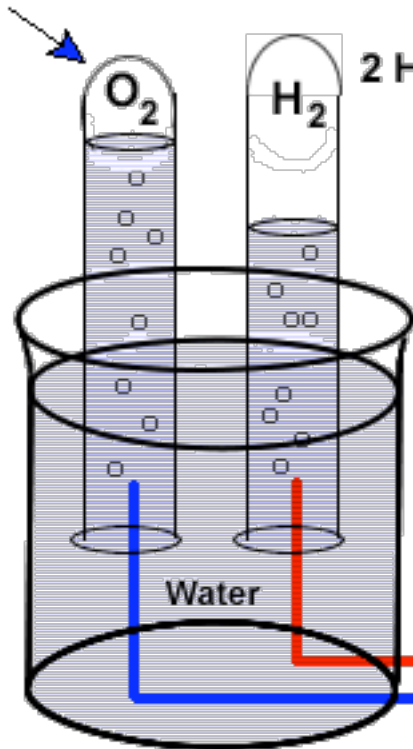
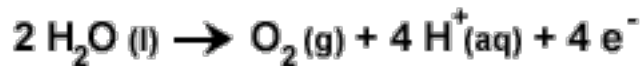


A viable solution to alternative and renewable energy

Hydrogen Production by Solar Water-Splitting



SOLAR WATER ELECTROLYSIS

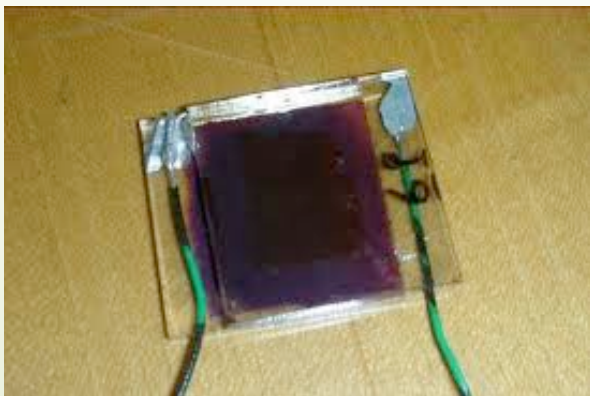


Solar Cell

$\Delta V = [1.23 + 0.8]$ Volts
Efficiency = 10%

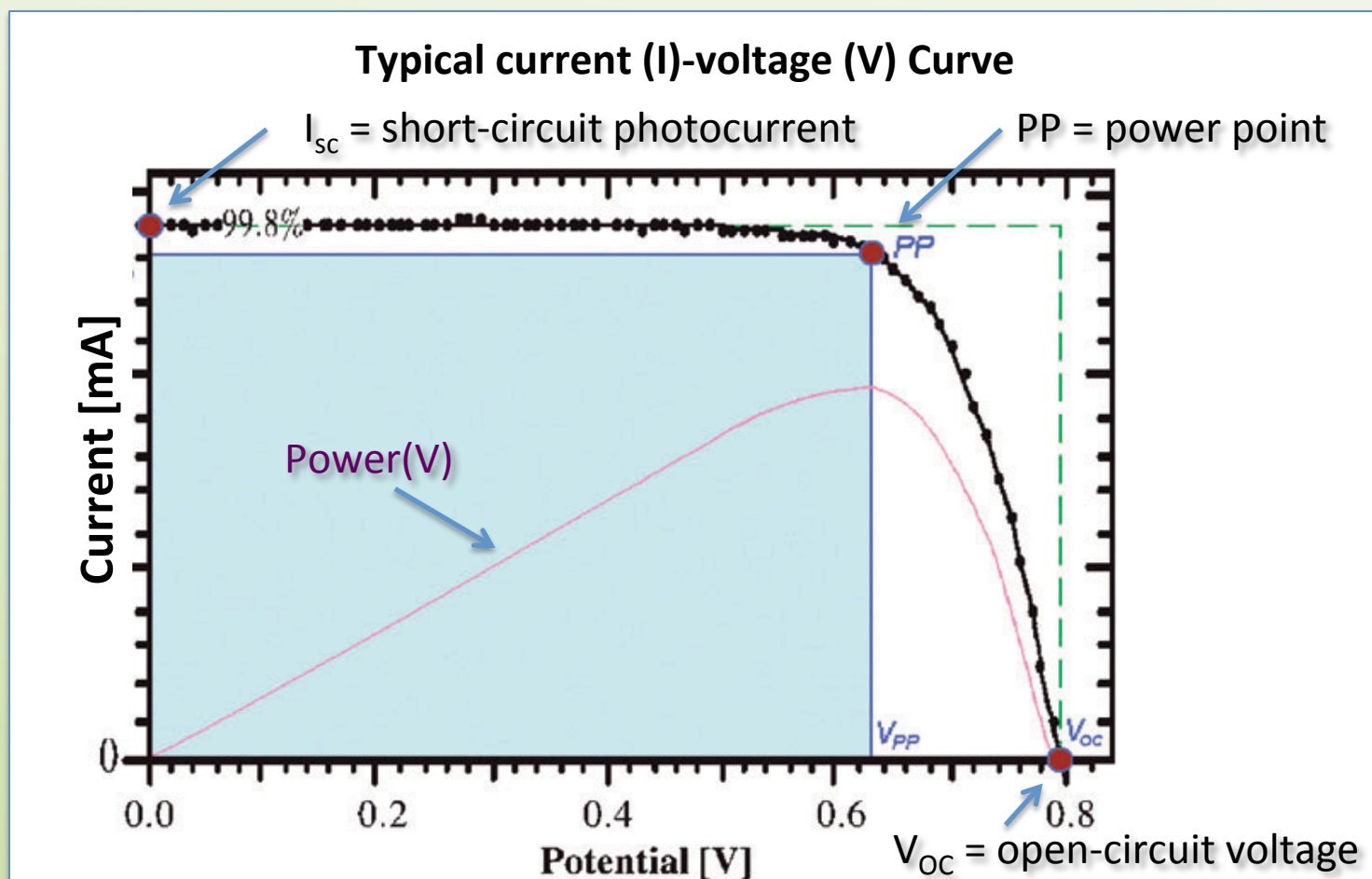
e^-

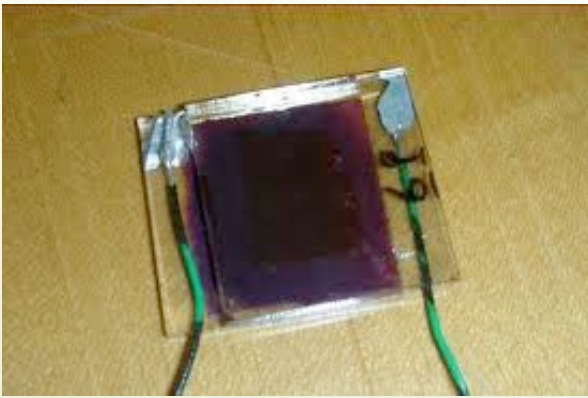
e^-



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Modeling Dye-Sensitized Solar Cells Characteristic I-V Curve of Photoconversion





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Modeling Dye-Sensitized Solar Cells

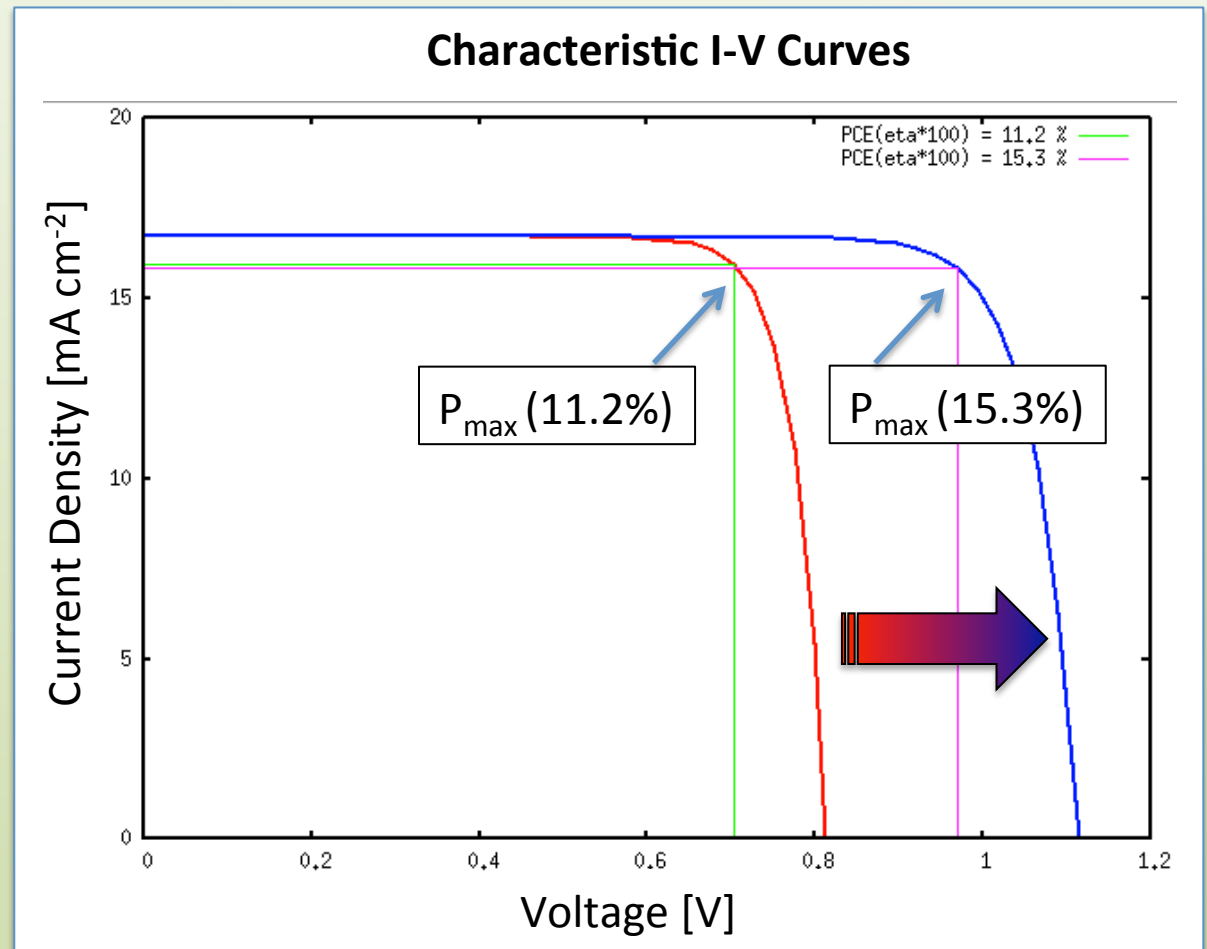
Photoconversion: Efficiency

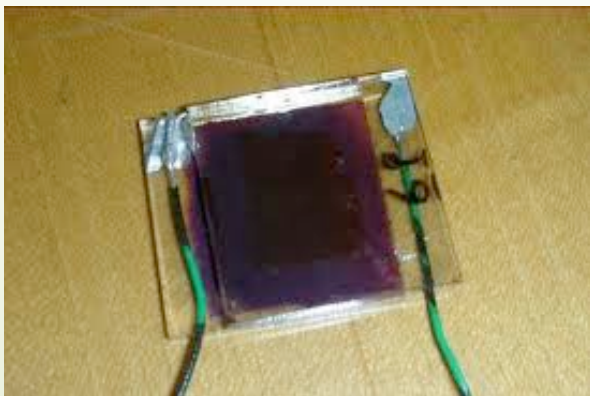
Power output

$$P_o = I \times V$$

**Light-to-electrical power
conversion % efficiency**

$$\eta = 100 \times P_o / P_i$$



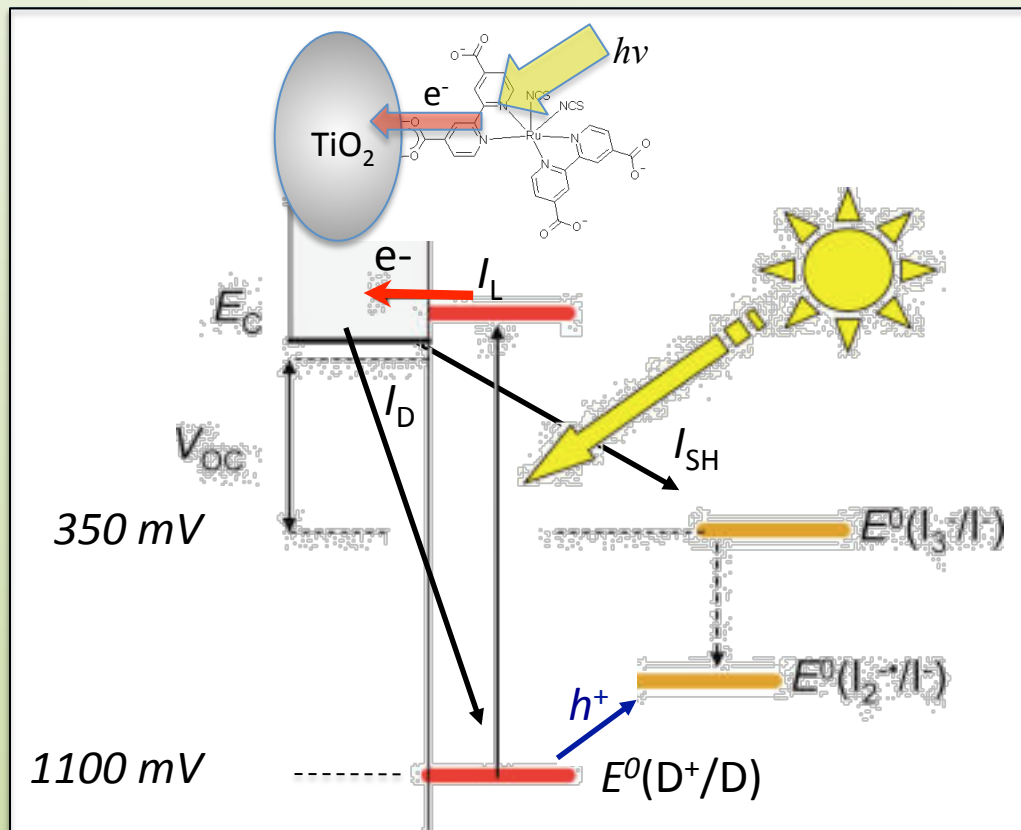


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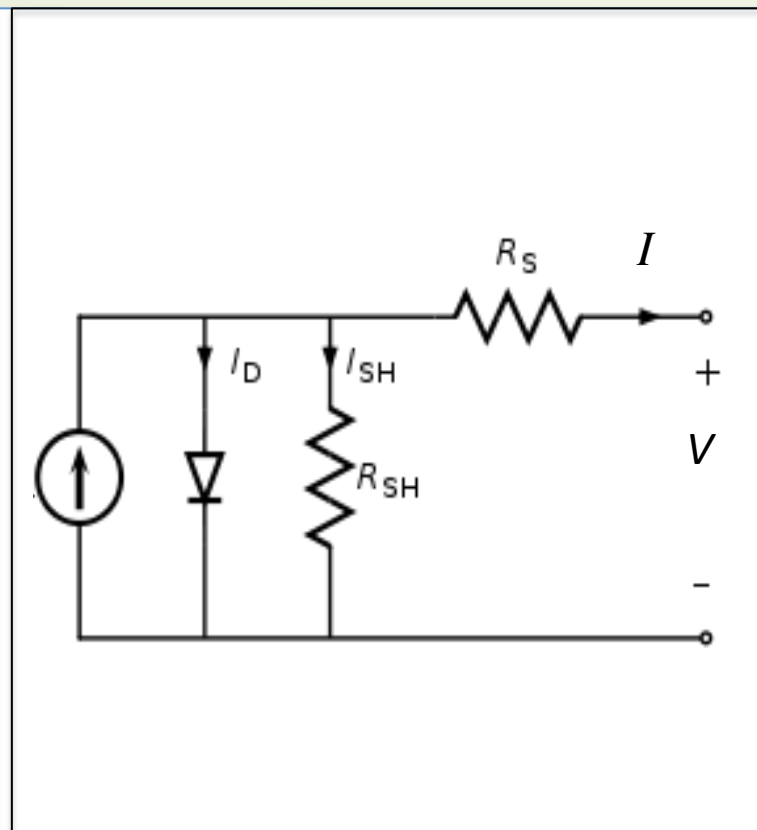
Modeling Dye-Sensitized Solar Cells

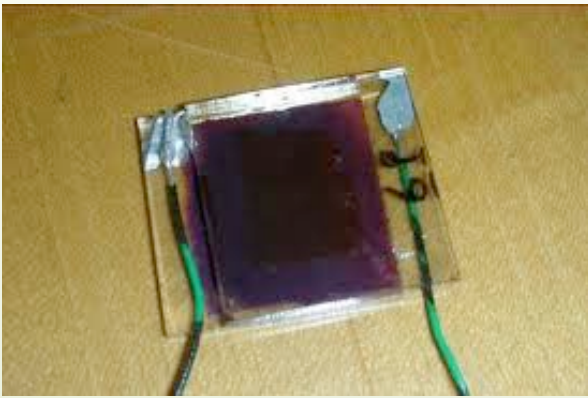
Equivalent Circuit of Photoconversion

Energy Diagram



Equivalent Circuit



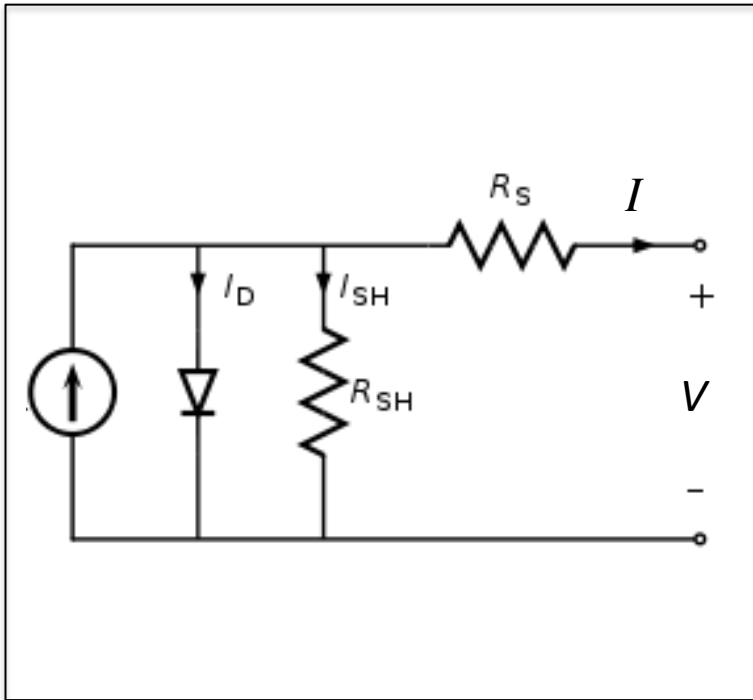


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Modeling Dye-Sensitized Solar Cells

Photoconversion: Output Current

Equivalent Circuit

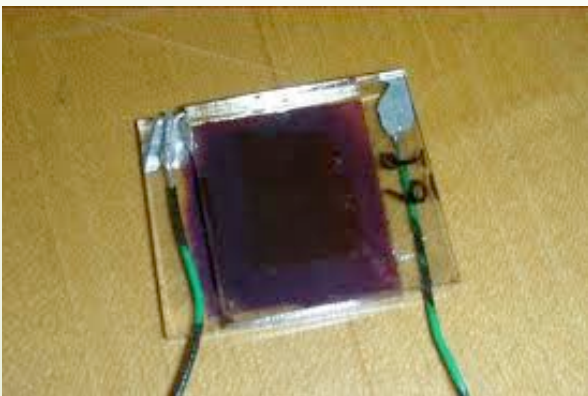


Characteristic I-V Curve

Output Current: $I = I_L - I_D - I_{SH}$

$$I = I_L - I_0 \left\{ \exp \left[\frac{q(V + IR_S)}{nkT} \right] - 1 \right\} - \frac{V + IR_S}{R_{SH}}$$

Open Circuit Voltage: $V_{OC} \approx \frac{kT}{q} \ln \left(\frac{I_L}{I_0} + 1 \right)$.



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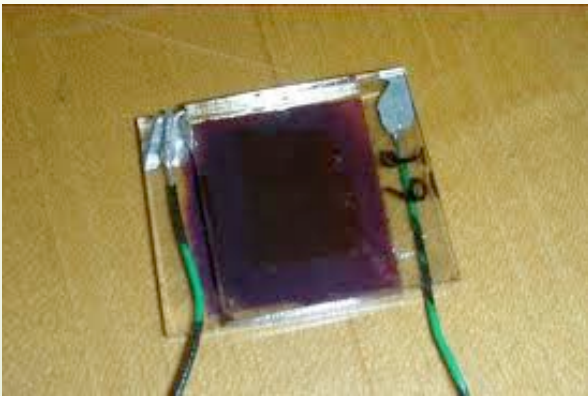
Modeling Dye-Sensitized Solar Cells
Photoconversion Efficiency: Redox Couple

Exercise 1 (due Thursday Sept 25, 2014):

Consider a dye-sensitized solar cell (DSSC) with an equivalent circuit with the following parameters:

- Photogenerated current density: $J_L = 16.7 \text{ mAmperes/cm}^2$
- Specific series resistance: $R_S = 2.0E-4 \text{ K}\Omega \cdot \text{cm}^2$
- Specific shunt resistance: $R_{SH} = 100 \text{ K}\Omega \cdot \text{cm}^2$
- Open circuit voltage (Volts): $V_{oc} = E^0(I^-/I_3^-) - E_{CB} + \Delta V(\text{pH})$
- Reverse saturation current density: $J_0 = J_L \cdot 10^{-10} \text{ mAmperes/cm}^2$
- Diode ideality factor times $kT/q = 0.0259 \text{ Volts}$: $nkt = V_{oc} / \log(J_L/J_0 + 1)$

- (a) Compute the I-V characteristic at $\text{pH} = 7.75$ assuming $E^0(I^-/I_3^-) = 350 \text{ mV}$, and $\Delta V(\text{pH}) = 60 \text{ mV} \cdot \text{pH} + E_{CB}$ relative to the hydrogen standard electrode (HSE).
- (b) Compute the light-to-electrical power conversion % efficiency (η) of the DSSC, assuming that incident sunpower $P_i = 1 \text{ kW m}^{-2}$.
- (c) Compute η for an analogous DSSC, where the redox couple I^-/I_3^- has been replaced by a redox pair X^-/X_3^- with $E^0(X^-/X_3^-) = 150 \text{ mV}$.



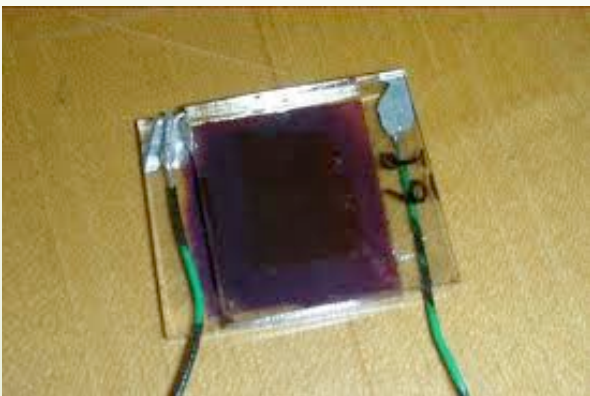
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Modeling Dye-Sensitized Solar Cells
Photoconversion Efficiency: Redox Couple

Solution to Exercise 1 (standard fortran):

```
PROGRAM main
PARAMETER(npt=100)
dv=2.4/(npt-1)
pmax=-1.
DO i=1,npt
  v=(i-1)*dv
  rv=rj(v,rkt)
  IF(rv.GT.(-10.0)) THEN
    p=v*rv
    PRINT *,p
    IF(p.GT.pmax) THEN
      pmax=p
      vmax=v
      rmax=rv
    END IF
    WRITE(10,22) v,rv
  END IF
END DO
PRINT *, "n(ideality factor)", rkt/0.0259
WRITE(11,22) 0,rmax
WRITE(11,22) vmax,rmax
WRITE(11,22) vmax,0.
PRINT *, "PCE(eta*100)=", pmax
22 FORMAT(2(e13.6,2x))
END
```

```
FUNCTION rj(v,rkt)
C
  rj1=16.7 ! current density
  rs=2.0E-4 ! specific series resistance
  rsha=100. ! specific shunt resistance
  Voc=0.42+0.35+0.045+0.3 ! Voc
  rj0=rj1*1.0E10 ! Rev. sat. curr. Density
C
  ideality factor times kT/q= 0.0259 Volts
  rkt=Voc/log(rj1/rj0+1.)
  DO i=1,5
    IF (i.EQ.1) rj=rj1
    rj=rj1-rj0*(exp((v+rj*rs)/rkt)-1.)
1    -(v+rj*rs)/rsha
  END DO
  RETURN
END
```



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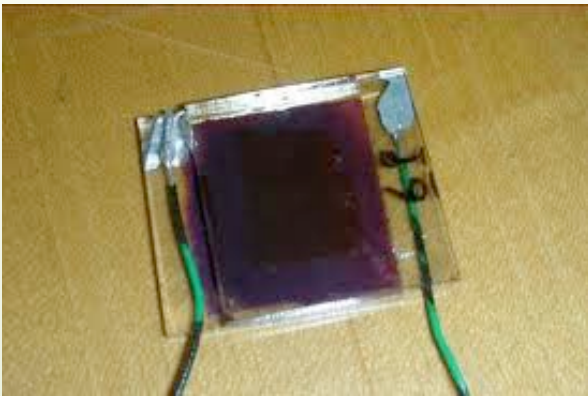
Conventional Solar Cells

Cost and Space Requirements

Exercise (Current Scenario) (due Thursday Sept 25, 2014):

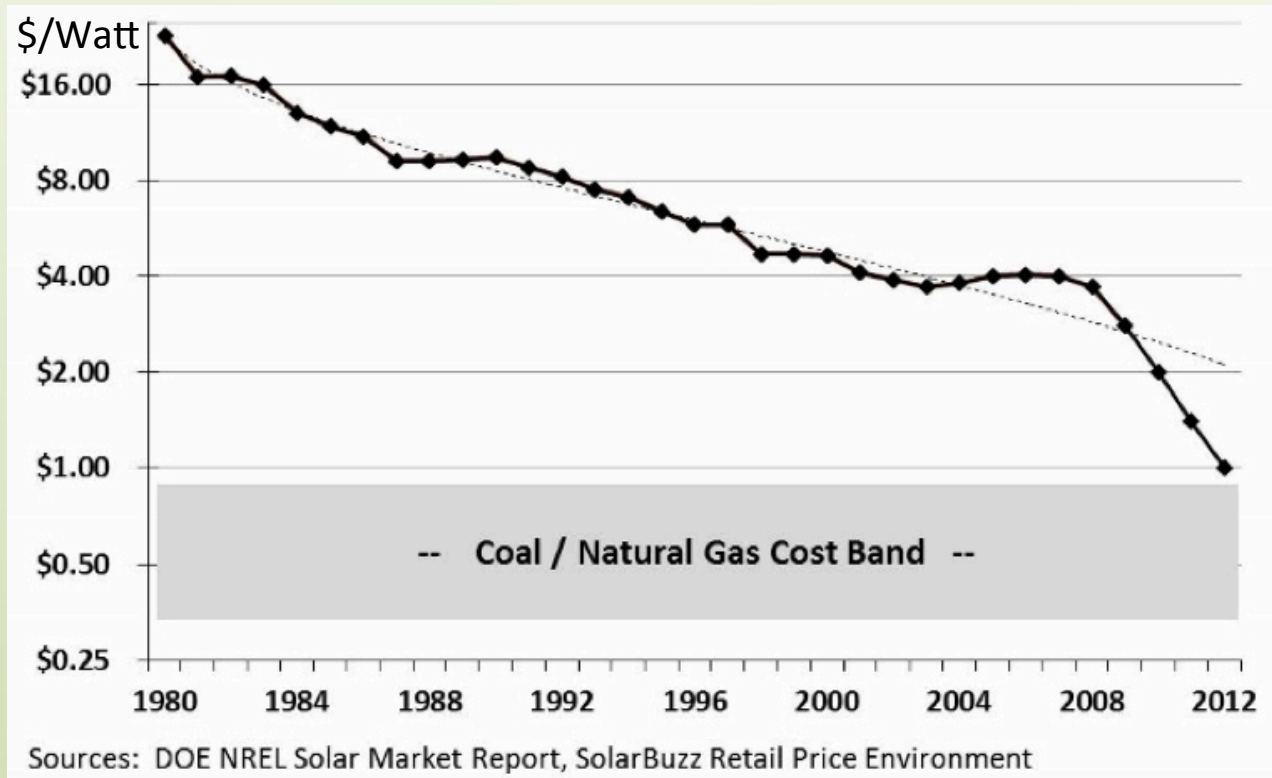
Considering that the current US energy consumption is at a rate of 3.5 TWatts:

- (1) What percentage of the US energy consumption is supplied by solar panels?
- (2) What percentage of the electricity in Germany is supplied by solar panels?
- (3) How much would the solar panels cost to supply the US with 3.5 Twatts?
- (4) How does that cost compare to the US military budget?
- (5) How much area would the solar panels take to supply 3.5 TWatts?
- (6) What percentage of the electricity in CT comes from nuclear reactors?
- (7) Where are the nuclear power plants?
- (8) When was the last time a hurricane hit the coast of CT?



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Plummeting Solar Module Cost PV Parity?

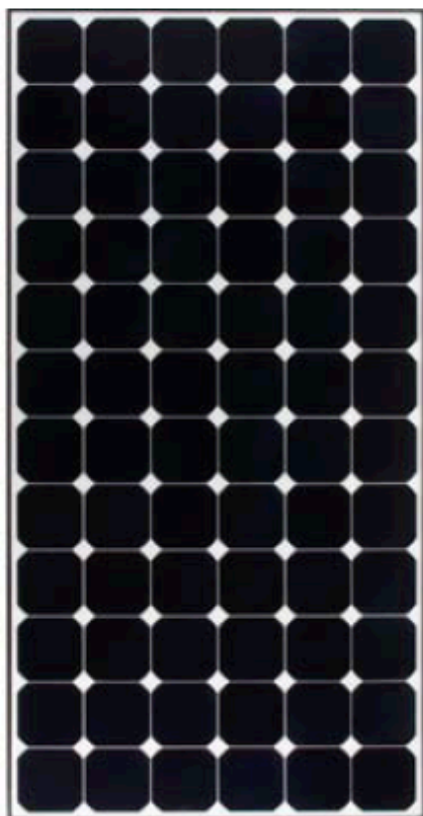


“what is certain is that we're headed for parity with fossil fuels (the gray area in the graph), and then solar will beat them...” [Michael Graham Richard](#), May 1, 2013

Considering \$1/Watt

230 SOLAR PANEL

EXCEPTIONAL EFFICIENCY AND PERFORMANCE



SUNPOWER

$$1 \text{ kWatt/m}^2 \cdot 18.5/100 = 185 \text{ W/m}^2$$

BENEFITS

Highest Efficiency

Panel efficiency of 18.5% is the highest commercially available for residential applications

$$11.2/0.185 = 60.5 \text{ m}^2 / \text{person}$$

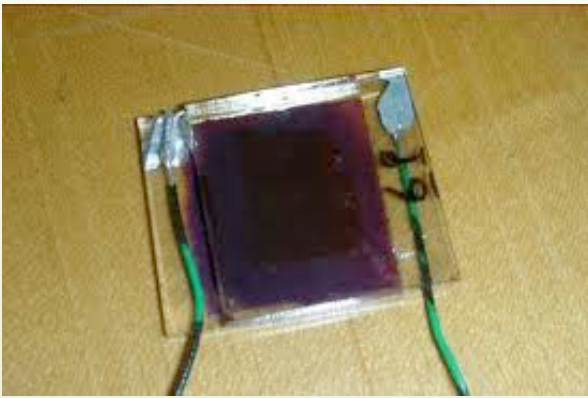
Solar Panel for Current U.S. Energy Consumption Size and Cost

- ✓ 11.2 KWatts/person = 3.5×10^{12} Watts (3.5 Twatts)
 - ✓ Cost of solar panels: \$11,200 /person = [\$3.5 Trillions]

2012 U.S. military budget = \$2,064/person [\$0.646 Trillion]

2011 Ivanpah BrightSource Energy = \$5.1/person

WASHINGTON (Army News Service, **July 8, 2010**) --"We view energy security as a critical mission-enabler and an operational imperative, which can provide the Army with an essential tactical advantage," said Jerry Hansen, the Army's senior energy executive, during a bloggers roundtable discussion, July 7, at the Pentagon. "Our Army installations, our tactical operations, Soldier training -- all require secure and uninterrupted access to energy."

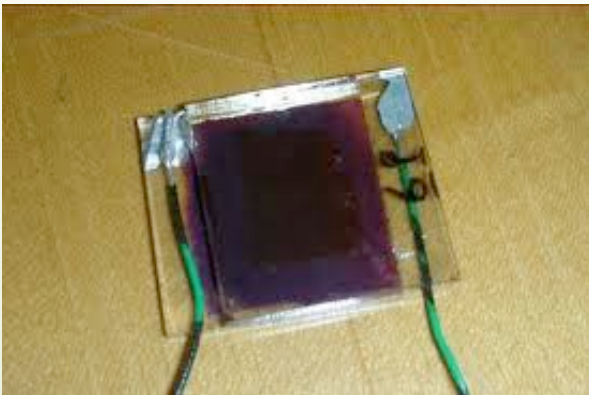


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Modeling Photovoltaic Solar Cells **U.S. Energy Consumption**

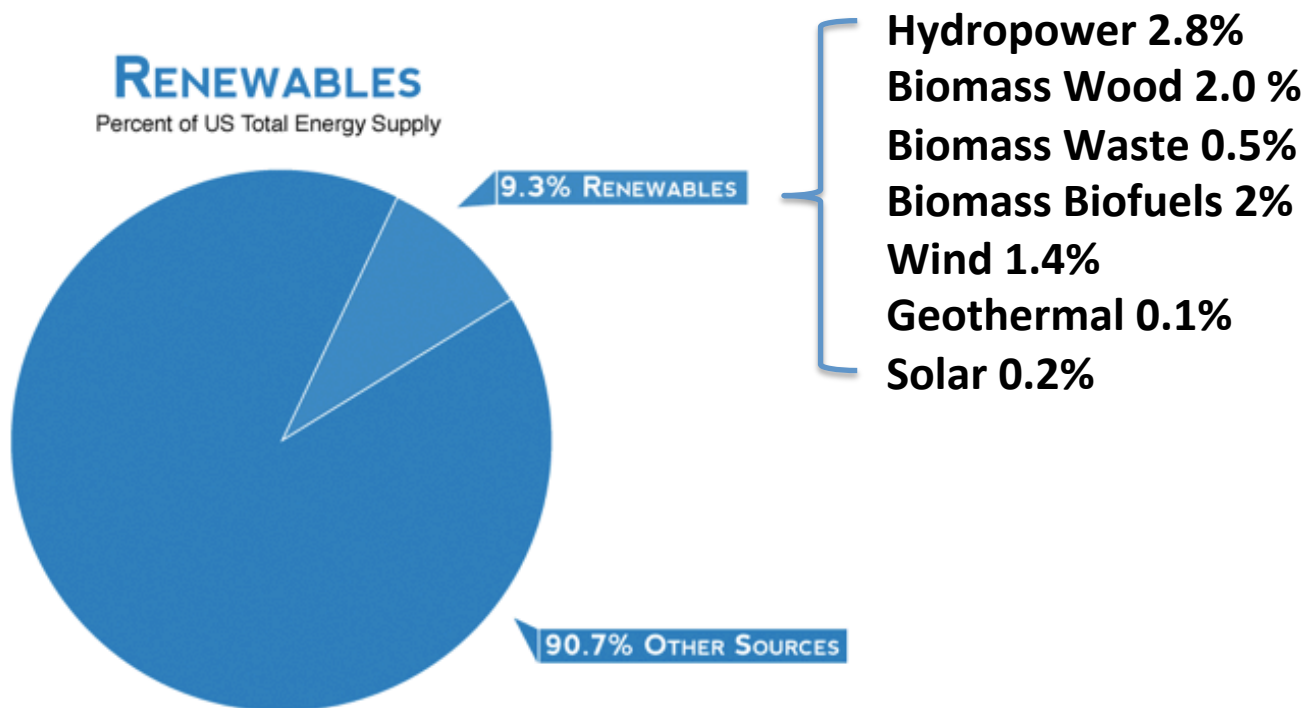
✓ 11.2 KWatts/person = (3.5 TWatts)

- Each person consumes energy, on average, at a rate comparable to the energy consumption of 11 window air conditioners, or 110 light bulbs (100 Watts each).
- Sunlight shines on earth at an average flux rate of 1.0 KWatt/m². Therefore, the average flux of solar energy shining on 11.2 m² (120 ft²) corresponds to the average energy consumption per capita.



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2012 U.S. Renewable Energy Consumption



Source: EIA, MER, April 2013 (6/26/13)

April 11, 2011. DOE Finalizes \$1.6 Billion Loan Guarantee for BrightSource Energy



IVANPAH: World's Largest Solar Thermal Plant



[As World's Largest Solar Thermal Plant Opens, California Looks to End Solar Wars](#)

July 12, 2013. In a few weeks, the largest solar plant of its kind in the world will start producing power in California's Mojave Desert.

The [Ivanpah Solar Electric Generating System](#) will supply both Northern and Southern California, inching the state one step closer to its ambitious renewable energy goal.